## Mastering the CALCULATOR

# USO <br> AUSTRALIA 

Cnsio fx. $82 \pi$

# MASTERING THE CALCULATOR USING THE CASIO fx-82TL 

Learning and Teaching Support Unit (LTSU) The Learning Centre

## Guide book

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## Introduction

This is one in a series of booklets prepared to assist students who are learning to use a calculator. They have been prepared by staff in The Learning Centre from Learning and Teaching Support Unit (LTSU) at USQ. The series comprises:

Mastering the calculator

- Using the Casio $f x$-100s (also suitable for Casio $f x-570$ )
- Using the Casio $f x$-100AU
- Using the Casio $f x-82 \mathrm{LB}$
- Using the Casio $f x-82 \mathrm{TL}$
- Using the Casio fx-82MS
- Using the Sharp EL-531LH
- Using the Sharp EL-556L
- Using the Sharp EL-531RH

The instructions in this booklet only explain some of the keys available on your calculator necessary for basic work in data manipulation. If you require more assistance please contact The Learning Centre. If you would like information about other support services available from The Learning Centre, please contact

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## A word about starting out

- Make sure you are in the correct mode selection and that all previous data is cleared.

MODE

- For e.g. To perform arithmetic operations press
- To clear all values press

```
ACION
```

- To clear memory press O STO M+
- If your calculator has FIX or SCI on the display press MODE ${ }^{\text {mree times }}$

appears on the screen
press 3 then 2 so you are in Normal mode.
- If your calculator has RAD or GRAD on the display press

MODE

appears on the screen
press 1 so you are in Degree mode.

## 1. Addition and subtraction

### 1.1 To add numbers



Find the + key
(it is shown on the photograph of the calculator here).

## Example

To add 7 and 3 , type


The display should read 10
Example
I want to find the total amount I earned in the past four weeks. If I earned \$471, \$575, \$471 and $\$ 528$, the key strokes would be


The display should read 2045.

### 1.2 Sometimes you make an error when typing in a number

If this happens use the DEL key to cancel the number and then type in the correct number and continue.

Example
If you want to enter $3+4$ but accidentally type $3+5$
press DEL to cancel the 5 .

Now type $4=$

Example
If I want to add 471 and 575 but I typed

## $4171+5176$

I can cancel 6 by typing DEL and then typing $5=$
The display should read 1046.
'Try practising cancelling with the DEL key until you are comfortable with its use.'

### 1.3 The $\xrightarrow{\text { aneman }}$ keys are used when you to delete other data

Example
If you typed:
$471+546$
but you wanted $471+576$
press the key twice. The 4 flashes. Press 7 . The 7 now replaces the 4 .

Press

The display should read 1047.
Practice using this key when replacing digits, operation keys ( $+-\times \div$ ), or more than one digit (use the DEL key).


If you typed $471+56$
but you wanted $471+576$, press


SHIFT ins
the display should read 1047.

### 1.4 To subtract numbers

Find the $\quad$ key (it is shown on the photograph of the calculator following).
Example
To subtract 35 from 257, type


The display should read 222


Example
$348-24-19$
The keystrokes are


The display should read 305 .
Sometimes you may have a sum like this:
$-7+4$
You can use the (-) key.
The key strokes are


The display should read -3.
You could also use the keystrokes


In this case the calculator recognises the - as a negative (not recommended to do it this way).

## 2. Multiplication and division

### 2.1 To multiply numbers

Find the $\times$ key (it is shown on the photograph of your calculator here).


## Example

To multiply 7 and 3 , type

```
7\times3}
```

The display should read 21
To find $753 \times 492$, type


The display should read 370476

### 2.2 To divide numbers

Find the $\div$ key (it is shown on the photograph of the calculator)
Example
To divide 35 by 7, type

## $35 \div 7=$

The display should read 5
To divide 7905 by 85, type

## $7905 \div 5=$

The display should read 93
To divide 56 by 23947 type

## $56 \div 2 \div 3.94=$

The display should read 0.002338497
If it reads $2.3385^{\times 10^{-03}}$ or something similar, then your calculator is in SCI (Scientific mode). See page 2 to change to NORM (normal mode).

### 2.3 Combining multiplication and division

Example
If the question is
$\frac{27}{7 \times 4}$ then
it is really $27 \div 7 \div 4$.
Try it.
The display should read 0.964285714

## 3. Brackets

Find the set of bracket keys on your calculator.
The $f x$-82TL allows you to use many sets of brackets.


## Example

Do the calculation $471-(93+11+2)$ on the calculator. (Make sure your calculation is in ordinary comp. mode press MODE
$\square$ 1)

The keystrokes required are


The display should read 365 .
Sometimes in calculations you will see other grouping symbols, for example, $\}$ (called braces), [ ] (called square brackets).

Try these examples:
Exercise 1
(a) $25+(7+2-4)$
(b) $18(3+7)$ [a multiplication sign is understood $18 \times(3+7)]$
(c) $4+5[2(3+7)]$ [to use two sets of brackets just press the same button]
(d) $\frac{5}{(3+2)}$

Answers: $\quad 30 ; 180 ; 104 ; 1$

## 4. Powers

### 4.1 Squaring and higher powers

$6^{2}$ means $6 \times 6$. You can use the square key to do this calculation. (It is shown on the photograph of your calculator here.)

the display should read 36 .
Or you can use the power key on your calculator.

Find the $x^{y}$ key on your calculator.
Example
To square 6 ,
that is, find $6^{2}$, type

## $6 x^{y} 2=$

The display should read 36
[The first number you put in is the 6. This is the $x$ and the second number you put in (2) is $y$. That is why it is called the $x^{y}$ key.]

To find $27^{3}$ the required key strokes are

and the display should read 19683.
If you have learnt your multiplication tables you will already know the squares of the whole numbers from 1 to 12 and thus be able to complete much of the following table.

## Exercise 2

Use your calculator to find the squares of the whole numbers from 13 to 25 and any other squares you are unsure of.

| $1^{2}=1$ | $11^{2}=$ | $21^{2}=$ |
| :--- | :--- | :--- |
| $2^{2}=4$ | $12^{2}=$ | $22^{2}=$ |
| $3^{2}=9$ | $13^{2}=$ | $23^{2}=529$ |
| $4^{2}=$ | $14^{2}=$ | $24^{2}=576$ |
| $5^{2}=$ | $15^{2}=$ | $25^{2}=625$ |
| $6^{2}=$ | $16^{2}=$ |  |
| $7^{2}=$ | $17^{2}=$ |  |
| $8^{2}=$ | $18^{2}=$ |  |
| $9^{2}=$ | $19^{2}=$ |  |
| $10^{2}$ | $20^{2}$ |  |

Exercise 3
You can use this key for other powers as well. Try these examples
(a) $7^{4}$
(b) $8^{10}$
(c) $(0.4)^{6}$ (you do not have to type the brackets in)
(d) $(-7)^{6}$ (you need to type the brackets in)
(e) $5^{0.4}$
(f) $5^{-4}$

Answers:
(a) 2401
(b) 1073741824
(c) $4.096 \times 10^{-3}$ or 0.004096 (you move the decimal 3 places to the left)
(d)

```
( (-) 7) xy 6 = 117649
```

(e) 1.903653939
(f) 0.0016 [Just press $5 x^{y}(-) \quad 4=5^{-4}$ is the same as


### 4.2 Square root

Finding the square root of a number 'undoes' or 'neutralises' the squaring of the number and vice versa. The symbol for square root is
$\sqrt{ }$ (This is called the radical sign)
The square root of 36 is written as $\sqrt{36}$
Now because $6^{2}=36, \sqrt{36}=6$.
Find the square root key on your calculator and type


The display will read 6.

What do you think $\sqrt{81}$ is? $\sqrt{81}=$

You should have said 9 because $9^{2}=81$
(Check your calculator)

What do you think $\sqrt{-49}$ will be? You should have said 'you can't find the square root of a negative' since you can't find a number that squares to give a positive. Your calculator will say Ma ERROR.

Exercise 4

Try these by looking at the table of squares you completed on the previous page and then check your answers on your calculator
(a) $\sqrt{16}=$
(e) $\sqrt{49}=$
(b) $\sqrt{144}=$
(f) $\sqrt{169}=$
(c) $\sqrt{100}=$
(g) $\sqrt{121}=$
(d) $\sqrt{441}=$
(h) $\sqrt{361}=$

The answers are $4,12,10,21,7,13,11,19$.
Let's now check that taking the square root neutralises squaring.
Try this on your calculator.
Find the square root of 3 squared that is, $\sqrt{3^{2}}$
The key strokes required are


The display should read 3
Because squaring and taking square roots are inverse operations, the order of the operatons can be reversed and the number is unaffected.

So the square, of the square root of 3 , should also equal 3
Try it on your calculator. The key strokes required are


Exercise 5
Complete the following without using the calculator
(a) $\sqrt{7}^{2}=$
(b) $\sqrt{7^{2}}=$
(c) $\sqrt{10^{2}}=$
(d) $\sqrt{\square}^{2}=10$
(e) $\sqrt{\square^{2}}=625$
(f) $\sqrt{\square}^{2}=144$
(g) $\sqrt{64}=\square$, because $8^{2}=\square$
(h) $\sqrt{121}=\square$, because $=121$
(i) $\sqrt{225}=\square$, because $=\square$

Check your answers on the calculator.

### 4.3 Other roots

You can also use the root key on the calculator. Find the $x^{y}$ on your calculator. To get to this key you must press shift first.


Look at the examples below.
Examples
(a) $9^{1 / 2}$

and the display should read 3 .
or

and the display should read 3 .
(b) $8^{\frac{1}{3}}$

and the display should read 2 .
(c) $16^{1 / 4}$

and the display should read 2 .
Note:

- Root key is a function at the back of the power key, so you will need to activate it with the SHIFT key
- See the key $\sqrt[x]{ }$. The $x$ stands for the root you want to take so it is typed first.
- From the examples above you may have seen that $8^{\frac{1}{3}}=\sqrt[3]{8} \cdot 8^{\frac{1}{3}}$ is called a fractional index.


## 5. Fractions

How do you add $\frac{1}{12}$ and $\frac{4}{63}$ ? Normally you would have to find a common denominator of
252.
So:
$\frac{1}{12}+\frac{4}{63}=\frac{21}{252}+\frac{16}{252}=\frac{37}{252}$

Or you can use your calculator to add fractions. Find the
$a \frac{b}{c}$ key


On the $a \frac{b}{c}$ key the ' $a$ ' represents the whole part of a mixed number and the $\frac{b}{c}$, represents the fraction part of a mixed number.

When the number you are typing is a proper or improper fraction the ' $a$ ' is zero and there is no need to type a value for it.

The key strokes required for the calculation $\frac{1}{12}+\frac{4}{63}$ are:
$1 a a^{b} / 2+4 a b 63=$
and the display will show $37 ل 252$ which is read as $\frac{37}{252}$
Example
Find $8 \frac{1}{9}+\frac{63}{72}$
Using the calculator the key strokes are:

## $8 a b / 1 a a b / 9+63 a b+2=$

and the display will show $8 \downharpoonleft 71 \downharpoonleft 72$ which is read as $8 \frac{71}{72}$
SHIFT
Note if you now press $a^{b} / \%$ the display will read $\frac{647}{72}$. So this key turns a mixed fraction into an improper fraction.

If you press the $a^{b} / \boldsymbol{c}$ key a second time the decimal equivalent is displayed, i.e. 8.9861111

## Example

Find $25^{\frac{3}{2}}$
(This means the square root of 25 cubed).

The calculator strokes are:

## $25 x^{y}(3 \mathrm{ab} \% 2)=$

The display should read 125 .

## 6. Using the $x^{-1}$ key



This is a very useful key in more complex calculations. Find the $\qquad$
$X^{-1}$ key on your calculator.
( $x^{-1}$ really means $\frac{1}{x}$; e.g. $7^{-1}=\frac{1}{7}$ )
Example
Look at this example
$\frac{4}{7}$ is the same as $4 \times \frac{1}{7}$ or $\frac{1}{7} \times 4$
You can input this in your calculator by pressing


The answer should be 0.571428571 . This would be the same as if you just typed $4 \div 7$

Take another example
$\frac{4}{(8+3) \times 7}$

Type:


The answer should be 0.051948051

## 7. Scientific notation

Sometimes you may have numbers expressed in scientific notation, i.e., $7.24 \times 10^{3}$ instead of 7240. When a number is multiplied by $10^{3}$, you move the decimal point three places to the right. You can do this on the calculator by using the EXP key.


Press $7 \cdot 2 \cdot 4 E X P 3=$ , the display should read 7240 .

If you want to multiply two numbers e.g. $8.34 \times 10^{-2} \times 4.28 \times 10^{5}$. Press

## $8 \cdot 3.4$ EXP ( $-2 \times 2 \times 2 \times 2 \times 5=$

and the display will read 35695.2
If you press ${ }^{\text {MODE MODE MODE }} 2$ O the display will read $3.569520000^{04}$ which means $3.56952 \times 10^{4}$. Pressing the mode three times gives you the display


The 2 puts the calculator in scientific notation. The calculator then asks SCI 0~9? This gives the option of how many digits are displayed. The $O$ gives you 10 digits. Notice a small sci appears in the screen.


MODE MODE MODE
If you press $\times 10^{4}$. This rounds the number to 4 digits.

Practise using the EXP and MODE ${ }^{\text {keys on your calculator }}$

## 8. Factorial $x$ !

Look at your calculator and find the key with the symbol $x$ ! on it. You will come across this symbol when doing the Binomial Distribution. This is called the factorial key.


3 ! means $3 \times 2 \times 1 \quad$ and $5!=5 \times 4 \times 3 \times 2 \times 1$
$3!=6$

$$
5!=120
$$

How many ways would you guess that we could arrange ten people? That is, how large would you estimate 10 ! to be? Use your calculator to find 10 ! You should get 3628800 .

$$
10!=10 \times 9 \times 8 \times \ldots \times 3 \times 2 \times 1
$$

(Thank goodness this can be done on the calculator.)

## 9. Using memory

To calculate the following it may be useful to use the memory key for each term:
Example:

$$
\frac{(9-16)^{2}}{16}+\frac{(23-16)^{2}}{16}+\frac{(17-16)^{2}}{16}
$$



To make sure memory is clear, first press

or

and make sure you are in normal calculation mode [may need to press mode 1].
A small $m$ appears in the display when you put something in memory.

To do the calculation above, press the following keys


- this puts the first term (3.0625) into the memory
then press

- this adds the second term (3.0625) into memory
then press

- this adds the third term 0.0625 to memory.

To find the answer press $R C L$
The answer should be 6.1875 .
Example 2
calculate the following:
$\frac{18}{\sqrt{17}}+\frac{17}{\sqrt{17}}+\frac{12}{\sqrt{17}}$

press the following keys:

your answer should be 11.39917438
(There are other memory keys in your calculator - the A to F keys, accessed by using SHIFT STO and RCL - try them yourselves.)

## 10. Statistics

### 10.1 Mean and standard deviation - single data

The formula for the mean is $x=\frac{\Sigma x}{n}$

The formulas for the sample standard deviation are

$$
\begin{array}{ll}
s=\sqrt{\frac{\Sigma\left(x_{i}-x\right)^{2}}{n-1}} & \text { (Theoretical formula) } \\
s=\sqrt{\frac{\Sigma x_{i}^{2}-\left(\Sigma x_{i}\right)^{2} / n}{n-1}} & \text { (Working formula) }
\end{array}
$$

Your calculator will calculate the mean and standard deviation for you (the population standard deviation $\sigma_{n}$ or the sample standard deviation $\sigma_{n-1}$ - in data calculations you will usually use the sample standard deviation.)

The differentiation between $\sigma$ and $s$ varies with different calculators. On the Casio $f x-82 \mathrm{TL}, \sigma$ is denoted by $\sigma_{\mathrm{n}}$ and $s$ is denoted by $\sigma_{n-1}$. The positions of these keys is shown on the diagram below.


To find the mean and standard deviation,
firstly you must access the statistics mode of the calculator by using the keys $\square^{\text {mODE }}$ followed by 2 SD will appear in the centre of the screen.

Note that once you are in the statistics mode, the keys shown within the blue lines and pink letters are active. There are 14 blue keys and 9 pink keys on the Casio $f x$ - 82 TL . Make sure you can locate them. Before starting any computations always clear the statistic's memories using Mcl. Press ${ }^{\text {SHIFT }}{ }^{\text {Mcl Scl }} \mathrm{ACON}^{\circ}=$

I will use the data set $\mathrm{A}(-5,2,3,4,11)$ to demonstrate the use of the calculator. Note that I SHIFT
have shown the use of the key where necessary.

Step 1: Input the observations.


Step 2: Check that the correct number of observations have been inputted. [Note this is shown on the inside cover of your calculator under statistical data.]

Press RCL hyp
The display should read 5.

Step 3: Display the mean
SHIFT
$1=$ and the display should read 3

Step 4: Display the standard deviation (assume the data set is a sample)
SHIFT
$3-3$ and the display should read 5.7008771

Example
Use your calculator to find the mean, standard deviation and variance for data set $\mathrm{B}:-18,1,3$, 9, 20.
(the variance is the square of the standard deviation)

After you are in the statistics mode and cleared the statistics memories, the keystrokes required are:

RCL hyp and the display will read 5

## SHIFT

$1=$ and the display will read 3
SHIFT
$3=$ and the display will read 13.87443693
$x^{2}$ and the display will read 192.5

The mean is 3 , the standard deviation is 13.87 and the variance is 192.5 .
The RCL button accesses a number of extra statistical functions. (M, Y and X you will rarely use in basic statistics.)
$(-)=\Sigma x^{2}$
$\sin ^{\mathrm{D}}=\Sigma y^{2}$
$\mathrm{M}^{\mathrm{M}}=\Sigma x^{3}$
B
$0,99=\Sigma x$

$$
\cos ^{\mathrm{E}}=\Sigma y
$$

$$
,^{Y}=\Sigma x^{2} y
$$

$$
\underset{\text { hyp }}{\mathrm{C}}=n
$$

$$
\tan ^{\mathrm{F}}=\Sigma x y
$$

$$
)^{x}=\Sigma x^{4}
$$

In the example below, the progressive calculations are shown simply to give you some understanding of the underlying processes - you should do one or two examples in detail and then check them by calculator.

### 10.2 Mean and standard deviation of frequency distribution

Given below is the frequency table for the weights ( kg ) of a random sample of 30 first year university female students. Find the standard deviation, the variance and the mean.

| Graduate's weight <br> $(\mathbf{k g})$ | Frequency | Cumulative <br> frequency |
| :---: | :---: | :---: |
| 60 | 2 | 2 |
| 61 | 14 | 16 |
| 62 | 8 | 24 |
| 63 | 1 | 25 |
| 64 | 5 | 30 |

The calculations needed to obtain the standard deviation without statistical keys for these data are:
$\Sigma x^{2}=60^{2} \times 2+61^{2} \times 14+62^{2} \times 8+63^{2}+64^{2} \times 5=114495$
$\Sigma x=60 \times 2+61 \times 14+62 \times 8+63+64 \times 5=1853$

$$
\begin{aligned}
s & =\sqrt{\frac{\Sigma x_{i}^{2}-\left(\Sigma x_{i}\right)^{2} / n}{n-1}} \\
& =\sqrt{\frac{114495-(1853)^{2} / 30}{29}}=\sqrt{\frac{114495-114453.6333}{29}}=\sqrt{1.4264}
\end{aligned}
$$

Thus: $\quad s=1.2 \mathrm{~kg}$ and $s^{2}=1.4 \mathrm{~kg}^{2}$

$$
\bar{x}=\frac{\Sigma x}{n}=\frac{1853}{30}=61.8 \mathrm{~kg}
$$

Note: In calculations like the above you should carry as many decimals as possible until the final result. The number of decimals to be retained at the end depends on the accuracy of the data values - one rule of thumb is to have one more decimal than in the original data.

Notice how the frequencies were used in the above calculation.
The calculator usage now has a small modification because we have been given the frequencies for the variable values. (There is no need to input each single observation.)

The keystrokes required are:


SHIFT ; ${ }^{-\cdots}$ SHIFT ; Y


RCL hyp and the display should read 30

SHIFT

$1=$ and the display should read 61.766667

## SHIFT


$3=$ and the display should read 1.1943353
$x^{2}=$ and the display should read 1.4264369

Thus, as expected

$$
s=1.2 \mathrm{~kg}, s^{2}=1.4 \mathrm{~kg}^{2} \text { and } x=61.8 \mathrm{~kg}
$$

Exercise 6
Find the mean, standard deviation and variance of
(a) The annual rainfall data for the years 1971-1990

| Year | $\mathbf{1 9 7 1}$ | $\mathbf{1 9 7 2}$ | $\mathbf{1 9 7 3}$ | $\mathbf{1 9 7 4}$ | $\mathbf{1 9 7 5}$ | $\mathbf{1 9 7 6}$ | $\mathbf{1 9 7 7}$ | $\mathbf{1 9 7 8}$ | $\mathbf{1 9 7 9}$ | $\mathbf{1 9 8 0}$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Rain <br> $(\mathbf{m m})$ | 1340 | 990 | 1120 | 1736 | 260 | 1100 | 1379 | 1125 | 1430 | 1446 |
| Year | $\mathbf{1 9 8 1}$ | $\mathbf{1 9 8 2}$ | $\mathbf{1 9 8 3}$ | $\mathbf{1 9 8 4}$ | $\mathbf{1 9 8 5}$ | $\mathbf{1 9 8 6}$ | $\mathbf{1 9 8 7}$ | $\mathbf{1 9 8 8}$ | $\mathbf{1 9 8 9}$ | $\mathbf{1 9 9 0}$ |
| Rain <br> $(\mathbf{m m})$ | 1459 | 1678 | 1345 | 978 | 1002 | 1110 | 1546 | 1672 | 1467 | 1123 |

(b) The sample of snail foot lengths

| Snail foot length (cm) |  |  |  |  |  |  |  |
| :--- | :--- | :--- | :---: | :---: | :---: | :---: | :---: |
| 2.2 | 4.1 | 3.5 | 4.5 | 3.2 | 3.7 | 3.0 | 2.6 |
| 3.4 | 1.6 | 3.1 | 3.3 | 3.8 | 3.1 | 4.7 | 3.7 |
| 2.5 | 4.3 | 3.4 | 3.6 | 2.9 | 3.3 | 3.9 | 3.1 |
| 3.3 | 3.1 | 3.7 | 4.4 | 3.2 | 4.1 | 1.9 | 3.4 |
| 4.7 | 3.8 | 3.2 | 2.6 | 3.9 | 3.0 | 4.2 | 3.5 |

Answers:
(a) Rainfall statistics
mean:

$$
\mu=1265.3 \mathrm{~mm}
$$

standard deviation:

$$
\sigma_{n-1}=336.4 \mathrm{~mm}
$$

variance:

$$
\sigma^{2}=113141.7 \mathrm{~mm}^{2}
$$

(b) Snail statistics
mean:

$$
\bar{x}=3.4 \mathrm{~cm}
$$

standard deviation:

$$
s=0.70 \mathrm{~cm}
$$

variance:

$$
s^{2}=0.49 \mathrm{~cm}^{2}
$$

## 11. Linear regression



## Example

Suppose we had a sample of 10 of the same type of banana. Their lengths and skin thicknesses were measured. Below is a summary of the results.

| Banana | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Length (mm) | 16.2 | 15.8 | 16.5 | 14.9 | 16.9 | 16.8 | 15.6 | 15.6 | 15.7 | 15.4 |
| Thickness (mm) | 1.1 | 1.2 | 1.1 | 1.0 | 0.9 | 1.2 | 1.1 | 1.2 | 0.9 | 0.8 |

## STEPS

1. To put the calculator into regression mode press ${ }^{\text {MODE }} 3$
2. Think of the sample of bananas as having two variables

- let $x$ be the variable length of banana
- let $y$ be the variable thickness of banana

For each banana you have to put in both numbers.

To put in the first set of numbers, press the following keys:

, is used for the 1st variable
$M+$. is used for the 2 nd variable

Continue in this manner


After you have input all the numbers, check to see you have 10 samples.
Press RCL hyp. The display should read 10

To find the linear regression equation in the form

$$
y=a+b x
$$

you need to find the value of $a$ and $b$. These keys are formed as A and B under the 8 keys. The ${ }^{r^{\mathrm{B}} \text { SHIFT }}$ button is used for all buttons with a blue $\rceil$ symbol under it.

Press ${ }^{\text {SHIFT }}{ }^{A}=$ a is 0.3651

$\therefore$ the equation is $y=0.3651+0.0430 x$


$$
r=0.1928
$$

There is not a high correlation between the thickness of bananas and the length of bananas tested.


You can also use the $\underbrace{\text { SHIFT }}_{+}$to predict the length, given the thickness.
Example

If 0.6 is the thickness


The display will read 5.46625
Similarly you can use ${ }^{\text {SHIFT }} \stackrel{\hat{y}}{-}$ to predict the thickness, given the length.
Example

If 12 mm is the length


The display will read 0.8807

## 12. Trigonometric functions

The keys involved are:


Important: Make sure that your calculator is in the correct mode. For example, if your calculator has R or G on the display and you wish to work in degrees, press mode twice and then select 1 for degrees. Your screen should now display D.

Example 1
In the right-angled triangle below, the length of the side opposite the $20^{\circ}$ angle needs to be calculated.


To find the length of the side labelled $x \mathrm{~cm}$, use

$$
\begin{aligned}
& \tan 20^{\circ}=\frac{x}{5} \\
& \Rightarrow x=5 \tan 20^{\circ}
\end{aligned}
$$

The keystrokes on the calculator are:


The display should read 1.819851171 , so the length of $x$ is about 1.8 cm .

## Example 2

In the right-angled triangle below, the length of the hypotenuse needs to be calculated.


To find the length of the side labelled $x \mathrm{~cm}$, use:
$\sin 20^{\circ}=\frac{7}{x}$
$\Rightarrow x=\frac{7}{\sin 20^{\circ}}$
The keystrokes on the calculator are:


The display should read 20.466631 , so the length of the hypotenuse is about 20.5 cm .
Example 3
Given the lengths of two of the sides in the right-angled triangle below, find the value of the angle $\theta$ in degrees:


1 cm

In the diagram, $\cos \theta=\frac{1}{2}$ so $\theta=\cos ^{-1}\left(\frac{1}{2}\right)$
To find the value of $\theta$, you need to use the $\cos ^{-1}$ key. The calculator keystrokes are:


Note: You must first get the value of the division by using the brackets.
Your display should read $60^{\circ}$. If it does not, check that you are in degree mode.

## 13. Exponential and logarithmic functions

There are two log keys on your calculator, with their associated exponential keys. The latter are accessed by first using the shift key:


The ' $\log$ ' key uses base 10 and the ' 1 n ' key uses base $e$ (natural logarithm).

## Example 1

Solve equation $2^{a}=20$
Taking logs of both sides;

$$
\begin{aligned}
& \log 2^{a}=\log 20 \\
& \Rightarrow a \log 2=\log 20 \\
& \Rightarrow a=\frac{\log 20}{\log 2}
\end{aligned}
$$

To find the value of $a$, the keystrokes are:

## $\log 20 \div \log 2=$

The display should read 4.3219281 .
So, $2^{4.32} \approx 20$. Confirm this by using the $x^{y}$ key.

## Example 2

Given $\log y=1.584$, find the value of $y$

$$
\begin{aligned}
\log y & =1.584 \\
\Rightarrow y & =10^{1.584}
\end{aligned}
$$

The $10^{x}$ key is above the log key. Hence the keystrokes are:

## $0^{\text {SHIFT }} \log 1=\cdot 5 \cdot 8 \cdot 4=$

The display should read 38.370725
Example 3 (harder)
Given $\log _{x} 6=1.5$, find the value of $x$

$$
\begin{aligned}
& \log _{x} 6=1.5 \\
\Rightarrow & \frac{\log 6}{\log x}=1.5 \\
\Rightarrow & \frac{\log 6}{1.5}=\log x
\end{aligned}
$$

To find $\log x$, the calculator keystrokes are:

## $\log 6 \div 1 \cdot 5=$

The display should read 0.5187675 .

Since this is the value of $\log x$, you still need to find $x$ where $x=10^{0.5187675}$
Without removing the answer of 0.5187675 on your display, press:


Your display should now read 3.3019272
Note: You could use the 'In' key instead of the 'log' key - the answer would still be the same. Try it!


## 14. Degrees, minutes, seconds

The key involved is


This key can be used for problems involving degrees, minutes and seconds or hours, minutes and seconds.

## Example 1

Suppose that you have a trigonometric problem where the angle involved is given in degrees and minutes. e.g. Find $x$ where $x=4 \times \sin 25^{\circ} 36^{\prime}$

The keystrokes involved are:

## $4 \times \sqrt{\sin } 2500936009=$

The display should show 1.728343 , so $x$ is approximately 1.73
Example 2
If you wish to convert an angle in degrees to its equivalent in degrees, minutes and seconds:
e.g. $34.88^{\circ}$, the keystrokes are:


The display should read $34^{\circ} 52^{\circ} 48$
Example 3
To find the sum of 5 hours 52 minutes 30 seconds and 7 hours 45 minutes 49 seconds:
The keystrokes are:

## 

The display should read $13^{\circ} 38^{\circ} 19$ which is 13 hours 38 minutes and 19 seconds.
To convert this number on the display into hours and the decimal part of an hour, press


09
The display should read 13.638611 (hours).

## Review calculator exercises

## 1. Perform the following calculations

(i) $(5+4) \times 3$
(ii) $12.5-8 \div 0.5$
(iii) $\frac{3 \times 6-8}{4}$
(iv) $\frac{12.8}{16.5-3.8}$
(v) $\frac{7 \times 0.41+17}{(4+7) \times 2}$
(vi) $\frac{2.4}{\frac{3}{4}}$
(vii) $\sqrt{145.6-17.2^{2} / 5}$
(viii) $\sqrt{345.6-17.2^{2}} / 5$
(ix) $25+\frac{3 \times 27}{1.02 \sqrt{30}}$
(x) $(4.1333-3.000) \pm 2.015 \sqrt{\frac{0.1366^{2}}{6}+\frac{0.2000^{2}}{6}}$
(xi) $\frac{(100-90)^{2}}{90}+\frac{(50-60)^{2}}{60}+\frac{(20-30)^{2}}{30}$
2. The following data is on growth (in $\$ \mathrm{~m}$ ) in an economy over a 8 year period:
$\begin{array}{llll}2.5 & 6.2 & -2.1 & 0.04\end{array}$
$8.2 \quad 7.4$
$2.1 \quad-1.7$

Calculate
(i) $\Sigma x$
(ii) $\Sigma x^{2}$
(iii) $(\Sigma x)^{2}$

Explain in words what each of these mean.

## Calculator solutions

1. 

(i) $(5+4) \times 3 \quad=27$

Make sure your calculation is in comp mode.
(ii) $12.5-8 \div 0.5$
$=-3.5$
(iii) $\frac{3 \times 6-8}{4}$

$$
=2.5
$$

Either $(3 \times 6-8) \div 4=$, or $3 \times 6-8=\div 4=$
(iv) $\frac{12.8}{16.5-3.8} \quad=1.007874$

Either $12.8 \div(16.5-3.8)=$, or $16.5-3.8=x^{-1} \times 12.8=$
(v) $\frac{7 \times 0.4+17}{(4+7) \times 2} \quad=0.9$

Either $\ldots \div((4+7) \times 2)=$ or $\ldots \div(4+7) \div 2=$
(vi) $\frac{2.4}{\frac{3}{4}}$
$=3.2$

Either $2.4 \div(3 \div 4)=$, or $2.4 \div 3 \mathrm{ab} / \mathrm{c} 4=$
(vii) $\sqrt{145.6-17.2^{2} / 5}$

$$
=9.296 \ldots
$$

Either $145.6-17.2 x^{2} \div 5=\sqrt{ }=$ or $\sqrt{ }\left(145.6-17.2 x^{2} \div 5\right)=$
(viii) $\sqrt{345.6-17.2^{2}} / 5$

$$
=1.41 . .
$$

Either $345.6-17.2 x^{2}=\sqrt{ }=\div 5=$, or $\left(345.6-17.2 x^{2}\right)=\sqrt{ }=\div 5$
(ix) $25+\frac{3 \times 27}{1.02 \sqrt{30}}$ $25+3 \times 27 \div 1.02 \div \sqrt{ } 30$
(x) $(4.1333-3.000) \pm 2.015 \sqrt{\frac{0.1366^{2}}{6}+\frac{0.2000^{2}}{6}} \quad=1.3325$ or 0.9341

Calculator keys: $\quad 0.1366 x^{2} \div 6+.2 x^{2} \div 6=\sqrt{ }=\mathrm{x} 2.015=\mathrm{M}+$

$$
\begin{aligned}
& +4.1333-3 \\
& =\text { AC } 4.1333-3-\text { RCL M+ }
\end{aligned}
$$

(xi) $\frac{(100-90)^{2}}{90}+\frac{(50-60)^{2}}{60}+\frac{(20-30)^{2}}{30} \quad=6.1111$

Calculator keys: $\quad(100-90) x^{2} \div 90+(50-60) x^{2} \div 60+(20-30) x^{2} \div 30=$
2. The following data is on growth (in $\$ \mathrm{~m}$ ) in an economy over a 8 year period:
$\begin{array}{llll}2.5 & 6.2 & -2.1 & 0.04\end{array}$
$\begin{array}{llll}8.2 & 7.4 & 2.1 & -1.7\end{array}$

Calculate
(i) $\Sigma x$
(ii) $\Sigma x^{2}$
(iii) $(\Sigma x)^{2}$ Explain in words what each of these mean.

To do this on the calculator, you must be in SD mode. Enter the data:
mode 2 2.5 M+6.2 M+2.1 (-) M+.04 M+8.2 M+7.4 M+2.1 M+1.7 (-) M+
(i) $22.64 \quad$ Press the key that says $\Sigma x(\underbrace{R C L} \stackrel{-}{\circ} \cdot \boldsymbol{B}$ )

This gives the total growth over the last 8 years
(ii) $178.4016 \quad$ Press the key that says $\Sigma x^{2}(R C L(-))$ This gives the sum of the squares of the growth in each year
(iii) 512.5696 Press $\Sigma x$ and $x^{2}$. This gives the square of the sum of the growth.

